

## 10.1.1 A simple expression grammar

### Description

In this section, we extend the grammar example with code to represent a complete grammar, a parser, and an evaluator. The reader may skip this section and the subsequent ones on the expression parser and the abstract syntax tree during the first reading of this book.

We use a grammar for describing arithmetic expressions of digits using '+', '\*' and parentheses:

```
Start: <Exp>
<Exp> ::= <Exp> "+" <Term> | <Term>
<Term> ::= <Term> "*" <Primary> | <Primary>
<Primary> ::= <Number> | "(" <Exp> ")"
<Number> ::= <Number> <Digit> | <Digit>
<Digit> ::= "0" | "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9"
```

The start symbol of the grammar is the nonterminal <Exp>.

The nonterminal symbols are: <Exp>, <Term>, <Primary>, <Number>, and <Digit>.

The terminal symbols are: "+", "\*", "(", ")" and the digits "0" – "9".

We declare an ExpressionGrammar as a sub of Grammar:

```
ExpressionGrammar: obj Grammar
  -- declaration of symbols
  -- declaration of rules
  -- specification of start symbol
```

The symbols are declared as follows:

```
expSy: obj Nonterminal("Exp")
termSy: obj Nonterminal("Term")
primarySy: obj Nonterminal("Primary")
numberSy: obj Nonterminal("Number")
digitSy: obj Nonterminal("Digit")
add: obj Terminal("+")
mult: obj Terminal("*")
leftB: obj Terminal("(")
rightB: obj Terminal(")")
```

To generate the rules, we introduce a method for each nonterminal. The one for <Exp> looks as follows:

```
mkExpRule: addRule(expSy)
  S: ref SymbolList
  S := SymbolList.insertList((ExpSy, add, termSy))
  R.alternatives.insert(Alternative(S))
  S := SymbolList.insertList(termSy)
  alt := Alternative(S)
  R.alternatives.insert(alt)
```

As can be seen, mkExpRule is a submethod of the method addRule, which we have added to class Grammar. In addition, we have added class SymbolList with a print method:

```
class Grammar:
  ...
  class SymbolList: OrderedList(#Symbol)
    print:
      scan
      current.print
```

```
addRule(L: ref Nonterminal):  
  R: ref Rule  
  R := Rule  
  R.leftSide := L  
  inner(addRule)  
  rules.insert(R)
```

The method `addRule` has the leftside of the rule to be added as a parameter `L`. It generates a `Rule`-object and assign its reference to `R`, and then assigns `L` to the `leftSide` of `R`. Then it executes `inner(addRule)` implying that the mainpart of `mkExpRule` is executed. When returning from `inner`, the `Rule R` is inserted into the list of rules.

The expression `SymbolList.insertList((ExpSy, add, termSy))` may need an explanation:

1. First `SymbolList` is evaluated creating a `SymbolList`-object returning a reference to this newly created object.
2. Then `insertList((ExpSy, add, termSy))` is invoked on the reference to the new `SymbolList`-object.
3. The parameter of `insertList` is an array and the argument of the invocation is the array-literal `(ExpSy, add, termSy)` – array-literal is introduced in section . `InsertList` inserts each element of the array in the newly generated `SymbolList`-object.

To complete the generation of `ExpressionGrammar`, we may add methods similar to `mkExpRule` for the other nonterminals, but leaves this an exercise for the reader. The `ExpressionGrammar` then looks as follows:

```
ExpressionGrammar: obj Grammar  
  -- declaration of symbols  
  ExpSy: obj Nonterminal("Exp")  
  ...  
  -- declaration of rules  
  mkExpRule: addRule(ExpSy)  
  ...  
  mkTermRule: addRule(TermSy)  
  ...  
  mkPrimaryRule: addRule(PrimarySy)  
  ...  
  mkNumberRule: addRule(NumberSy)  
  ...  
  mkDigitRule: addRule(DigitSy)  
  ...  
  -- specification of start symbol  
  start := ExpSy  
  mkExpRule  
  ...
```

## Parser and abstract syntax tree

Next we show how to write a parser for the expressions of our grammar and how to represent an expression by means of an abstract syntax tree. The reader may skip these sections during a first reading.